

## Math 10 - Homework Chapter 11 Answers

1. A bicycle safety organization claims that fatal bicycle accidents are uniformly distributed throughout the week. The table shows the day of the week for which 911 randomly selected fatal bicycle accidents occurred. At  $\alpha = 0.10$ , can you reject the claim that the distribution is uniform?

| <p><b>(a) (DESIGN)</b> State your Hypothesis</p> <p><b>Ho:</b> <math>p_1=p_2=p_3=p_4=p_5=p_6=p_7</math><br/> <b>Ha:</b> at least on <math>p_i</math> is different.</p>   | <p><b>(d) (DATA)</b> Conduct the test and <b>circle</b> your decision</p> <table border="1" data-bbox="792 451 1446 800"> <thead> <tr> <th>Survey</th> <th>Observe</th> <th>pi</th> <th>Expected</th> <th>ChiSq</th> </tr> </thead> <tbody> <tr> <td>Sunday</td> <td>118</td> <td>0.143</td> <td>130.143</td> <td>1.133</td> </tr> <tr> <td>Monday</td> <td>119</td> <td>0.143</td> <td>130.143</td> <td>0.954</td> </tr> <tr> <td>Tuesday</td> <td>127</td> <td>0.143</td> <td>130.143</td> <td>0.076</td> </tr> <tr> <td>Wednesday</td> <td>137</td> <td>0.143</td> <td>130.143</td> <td>0.361</td> </tr> <tr> <td>Thursday</td> <td>129</td> <td>0.143</td> <td>130.143</td> <td>0.010</td> </tr> <tr> <td>Friday</td> <td>146</td> <td>0.143</td> <td>130.143</td> <td>1.932</td> </tr> <tr> <td>Saturday</td> <td>135</td> <td>0.143</td> <td>130.143</td> <td>0.181</td> </tr> <tr> <td><b>Total</b></td> <td><b>911</b></td> <td><b>0.143</b></td> <td><b>911.000</b></td> <td><b>4.648</b></td> </tr> </tbody> </table> <p style="text-align: center;"><b>4.648 &lt; 10.645</b><br/> <b>Fail to Reject Ho</b></p> | Survey       | Observe        | pi           | Expected | ChiSq | Sunday | 118 | 0.143 | 130.143 | 1.133 | Monday | 119 | 0.143 | 130.143 | 0.954 | Tuesday | 127 | 0.143 | 130.143 | 0.076 | Wednesday | 137 | 0.143 | 130.143 | 0.361 | Thursday | 129 | 0.143 | 130.143 | 0.010 | Friday | 146 | 0.143 | 130.143 | 1.932 | Saturday | 135 | 0.143 | 130.143 | 0.181 | <b>Total</b> | <b>911</b> | <b>0.143</b> | <b>911.000</b> | <b>4.648</b> |
|--|---|--------------|----------------|--------------|----------|-------|--------|-----|-------|---------|-------|--------|-----|-------|---------|-------|---------|-----|-------|---------|-------|-----------|-----|-------|---------|-------|----------|-----|-------|---------|-------|--------|-----|-------|---------|-------|----------|-----|-------|---------|-------|--------------|------------|--------------|----------------|--------------|
| Survey   | Observe   | pi           | Expected       | ChiSq        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| Sunday   | 118   | 0.143        | 130.143        | 1.133        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| Monday   | 119   | 0.143        | 130.143        | 0.954        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| Tuesday  | 127   | 0.143        | 130.143        | 0.076        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| Wednesday  | 137   | 0.143        | 130.143        | 0.361        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| Thursday   | 129   | 0.143        | 130.143        | 0.010        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| Friday   | 146   | 0.143        | 130.143        | 1.932        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| Saturday   | 135   | 0.143        | 130.143        | 0.181        |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| <b>Total</b>   | <b>911</b>  | <b>0.143</b> | <b>911.000</b> | <b>4.648</b> |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| <p><b>(b) (DESIGN)</b> State Significance Level of the test and explain what it means.</p> <p><math>\alpha = .10</math>, the maximum probability of making Type I error, which would be incorrectly claiming bike accidents are not uniformly distributed.</p> | <p><b>(e) (CONCLUSION)</b> State your overall conclusion in language that is clear, relates to the original problem and is consistent with your decision.</p> <p><b>Insufficient evidence to conclude that bicycle accidents are not uniformly distributed.</b></p>   |              |                |              |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |
| <p><b>(c) (DESIGN)</b> Determine the statistical model .<br/> Determine decision rule (critical value method)</p> $\chi^2 = \frac{(O_i - E_i)^2}{E_i}$ <p>df = 6</p> <p><b>Reject Ho if <math>\chi^2 &gt; 10.645</math></b></p>                                |   |              |                |              |          |       |        |     |       |         |       |        |     |       |         |       |         |     |       |         |       |           |     |       |         |       |          |     |       |         |       |        |     |       |         |       |          |     |       |         |       |              |            |              |                |              |

2. Results from a survey five years ago asking where coffee drinkers typically drink their first cup of coffee are shown in the graph. To determine whether this distribution has changed, you randomly select 581 coffee drinkers and ask each where they typically drink their first cup of coffee. The results are shown in the table. Can you conclude that there has been a change in the claimed or expected distribution? Use  $\alpha = 0.05$ .

| <p><b>(a) (DESIGN)</b> State your Hypothesis</p> <p><b>Ho:</b> <math>p_1=.70</math> <math>p_2=.17</math> <math>p_3=.08</math> <math>p_4=.05</math><br/> <b>Ha:</b> at least on <math>p_i</math> is different</p>  | <p><b>(d) (DATA)</b> Conduct the test and <b>circle</b> your decision</p>   |        |               |              |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |
|---|---|--------|---------------|--------------|----------|-------|------|-----|-----|--------|-------|------|-----|------|-------|-------|---------|----|------|-------|-------|------------|----|------|-------|-------|--------------|------------|--|---------------|--------------|
| <p><b>(b) (DESIGN)</b> State Significance Level of the test and explain what it means.</p> <p><math>\alpha=.05</math>, the maximum probability of making Type I error, which would be incorrectly claiming that there has been a change in coffee drinking.</p> | <div data-bbox="747 310 1169 598" data-label="Figure"> </div> <table border="1" data-bbox="730 640 1421 882"> <thead> <tr> <th>Survey</th> <th>Observe</th> <th><math>p_i</math></th> <th>Expected</th> <th>ChiSq</th> </tr> </thead> <tbody> <tr> <td>Home</td> <td>389</td> <td>0.7</td> <td>406.70</td> <td>0.770</td> </tr> <tr> <td>Work</td> <td>110</td> <td>0.17</td> <td>98.77</td> <td>1.277</td> </tr> <tr> <td>Commute</td> <td>55</td> <td>0.08</td> <td>46.48</td> <td>1.562</td> </tr> <tr> <td>Rest/Other</td> <td>27</td> <td>0.05</td> <td>29.05</td> <td>0.145</td> </tr> <tr> <td><b>Total</b></td> <td><b>581</b></td> <td></td> <td><b>581.00</b></td> <td><b>3.754</b></td> </tr> </tbody> </table> <p style="text-align: center;"><math>3.754 &lt; 7.815</math><br/>Fail to Reject Ho</p> | Survey | Observe       | $p_i$        | Expected | ChiSq | Home | 389 | 0.7 | 406.70 | 0.770 | Work | 110 | 0.17 | 98.77 | 1.277 | Commute | 55 | 0.08 | 46.48 | 1.562 | Rest/Other | 27 | 0.05 | 29.05 | 0.145 | <b>Total</b> | <b>581</b> |  | <b>581.00</b> | <b>3.754</b> |
| Survey  | Observe   | $p_i$  | Expected      | ChiSq        |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |
| Home  | 389   | 0.7    | 406.70        | 0.770        |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |
| Work  | 110   | 0.17   | 98.77         | 1.277        |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |
| Commute   | 55  | 0.08   | 46.48         | 1.562        |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |
| Rest/Other  | 27  | 0.05   | 29.05         | 0.145        |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |
| <b>Total</b>  | <b>581</b>  |        | <b>581.00</b> | <b>3.754</b> |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |
| <p><b>(d) (DESIGN)</b> Determine the statistical model .<br/> Determine decision rule (critical value method)</p> $\chi^2 = \frac{(O_i - E_i)^2}{E_i}$ <p>df = 3</p> <p><b>Reject Ho if <math>\chi^2 &gt; 7.815</math></b></p>                                  | <p><b>(e) (CONCLUSION)</b> State your overall conclusion in language that is clear, relates to the original problem and is consistent with your decision</p> <p><b>Insufficient evidence to conclude that coffee drinking habits have changed.</b></p>  |        |               |              |          |       |      |     |     |        |       |      |     |      |       |       |         |    |      |       |       |            |    |      |       |       |              |            |  |               |              |

3. In a recent SurveyUSA poll, 500 Americans adults were asked if marijuana should be legalized. The results of the poll were cross tabulated as shown in the contingency tables below. Conduct **two** tests for independence to determine if opinion about legalization of marijuana is dependent on gender or age

Ho: Opinion on Marijuana Legalization and Gender are independent.

Ha: Opinion on Marijuana Legalization and Gender are dependent.

Model: Chi-square test of independence, 1 df. I will use  $\alpha = .05$

|                     |                 | Male   | Female     | Total  | Since p-value<.05, Reject Ho<br><br>Women are less likely to support marijuana legalization. |
|---------------------|-----------------|--|------------|--------|--|
| Should be Legal     | Observed        | <b>123</b>   | <b>90</b>  | 213    |  |
|                     | Expected        | 106.50   | 106.50     | 213.00 |  |
|                     | $(O - E)^2 / E$ | 2.56   | 2.56       | 5.11   |  |
| Should Not be Legal | Observed        | <b>127</b>   | <b>160</b> | 287    |  |
|                     | Expected        | 143.50   | 143.50     | 287.00 |  |
|                     | $(O - E)^2 / E$ | 1.90   | 1.90       | 3.79   |  |
| Total               | Observed        | 250  | 250        | 500    |  |
|                     | Expected        | 250.00   | 250.00     | 500.00 |  |
|                     | $(O - E)^2 / E$ | 4.45   | 4.45       | 8.91   |  |
|                     |                 | chi-square<br>8.91<br>1 df<br><b>.0028</b> p-value |            |        |  |

Ho: Opinion on Marijuana Legalization and age are independent.

Ha: Opinion on Marijuana Legalization and age are dependent.

Model: Chi-square test of independence, 2 df. I will use  $\alpha = .05$

|                     |                 | 18-34   | 35-54      | 55+       | Total  | Since p-value<.05, Reject Ho<br><br>Younger people are more likely to support legalizing marijuana. |
|---------------------|-----------------|---|------------|-----------|--------|---|
| Should be Legal     | Observed        | <b>95</b>   | <b>83</b>  | <b>48</b> | 226    |   |
|                     | Expected        | 72.32   | 94.47      | 59.21     | 226.00 |   |
|                     | $(O - E)^2 / E$ | 7.11  | 1.39       | 2.12      | 10.63  |   |
| Should Not be Legal | Observed        | <b>65</b>   | <b>126</b> | <b>83</b> | 274    |   |
|                     | Expected        | 87.68   | 114.53     | 71.79     | 274.00 |   |
|                     | $(O - E)^2 / E$ | 5.87  | 1.15       | 1.75      | 8.77   |   |
| Total               | Observed        | 160   | 209        | 131       | 500    |   |
|                     | Expected        | 160.00  | 209.00     | 131.00    | 500.00 |   |
|                     | $(O - E)^2 / E$ | 12.98   | 2.54       | 3.87      | 19.39  |   |
|                     |                 | chi-square<br>19.39<br>2 df<br><b>.0001</b> p-value |            |           |        |   |